

$$a) \sin(-x) = \frac{-2}{3} \quad \tan(x) = \frac{-2\sqrt{5}}{5}$$

$$\sin x = \frac{2}{3} \quad \csc x = \frac{3}{2}$$

$$\text{opp} = 2 \quad \text{adj} = -\sqrt{5} \quad \text{hyp} = 3$$

$$\cot(x) = \frac{-2\sqrt{5}}{5} = \frac{5\sqrt{5}}{-10} = \frac{-\sqrt{5}}{2} \rightarrow \frac{\text{adj}}{\text{opp}}$$

$$\cos x = \frac{-\sqrt{5}}{3} \quad \sec x = \frac{3}{-\sqrt{5}} = \frac{-3\sqrt{5}}{5}$$

14) $\tan \theta$ is undefined $\sin \theta > 0$

$$\text{opp} = 1 \quad \text{adj} = 0 \quad \text{hyp} = +1$$

$$\tan = \frac{\text{opp}}{\text{adj}} = \frac{1}{0}$$

$$1^2 + 0^2 = c^2$$

$$1^2 = c^2$$

$$\pm 1 = c$$

$$\sin \theta = 1$$

$$\csc \theta = 1$$

$$\cos \theta = 0$$

$$\sec \theta = \frac{1}{0} = \text{und.}$$

$$\tan \theta = \frac{1}{0} = \text{und}$$

$$\cot \theta = 0$$

Pythagorean Identities

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

Simplify

$$(\sin x)(\cos^2 x) - \sin x$$

$$(\sin x)(\cos^2 x - 1)$$

$$(\sin x)(-\sin^2 x)$$

$$-\sin^3 x$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\sin^2 \theta = -\cos^2 \theta + 1$$

$$\sin^2 \theta = 1 - \cos^2 \theta$$

$$-\sin^2 \theta = \cos^2 \theta - 1$$

$$a^m \cdot a^n = a^{m+n}$$

$$(1 - \cos^2 x)(\csc x)$$

$$(\sin^2 x)(\csc x)$$

$$(\sin^2 x)\left(\frac{1}{\sin x}\right)$$

$$\frac{\sin^2 x}{\sin x} = \sin x$$

$$\begin{array}{r} \sin^2 \theta + \cos^2 \theta = 1 \\ \cdot \cos^2 \theta - \cos^2 \theta \\ \hline \sin^2 \theta = 1 - \cos^2 \theta \end{array}$$

$$(\sin x) (\cot x)$$

$$(\sin x) \left(\frac{1}{\tan x} \right)$$

$$\frac{(\sin x)}{1} \left(\frac{\cos x}{\sin x} \right)$$

$$\frac{(\cancel{\sin x})(\cos x)}{\cancel{\sin x}}$$

$$\cos x$$

Verify

$$\frac{\sin x}{1 + \cos x} + \frac{\cos x}{\sin x} = \csc x$$

$$\frac{(\sin x)(\sin x) + \cos x(1 + \cos x)}{(1 + \cos x)(\sin x)}$$

$$\frac{\sin^2 x + \cos x + \cos^2 x}{(1 + \cos x)(\sin x)}$$

$$\frac{1 + \cos x}{(1 + \cos x)(\sin x)} = \frac{1}{\sin x} = \csc x$$

Homework

Pg. 345 #15-20

$$\frac{12(4)}{3(4)} +$$

$$\frac{3(3)}{4(3)} \rightarrow$$

$$\frac{\quad}{12}$$